

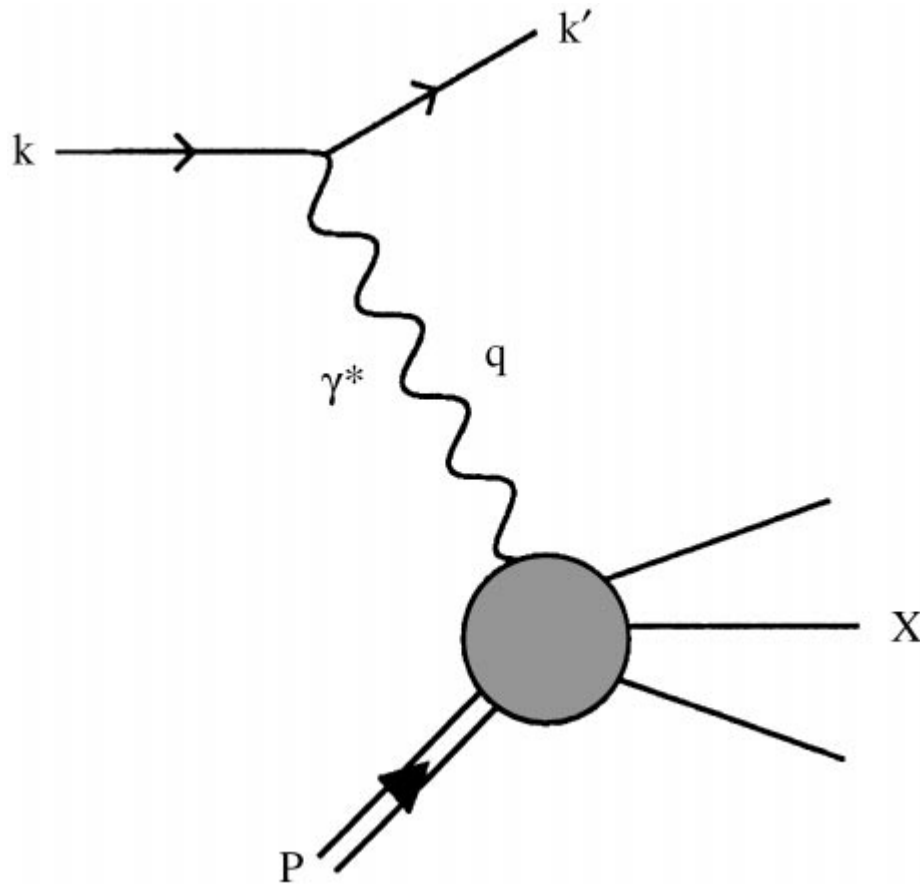
Nuclear structure functions

TUS K. Saito

- DIS kinematics — what can we see in DIS ?
- Experiments — what is the nuclear EMC effect ?
- Theoretical approaches — can we understand it ?
- Possible explanations — what do we need ?
- Summary



1. Kinematics of Deep Inelastic Scattering (DIS)



- Initial and final lepton 4-momentum:
 $k^\mu, k'^\mu, k^2 = k'^2 = m^2 \approx 0$
- Virtual photon 4-momentum squared:
 $q^2 = (k - k')^2 \equiv -Q^2 < 0$
- Initial nucleon (nucleus) 4-momentum:
 $P^\mu = (E_T, \vec{P}), P^2 = M_T^2$
- Final hadronic 4-momentum squared:
 $P_X^2 = (P + q)^2 \equiv W^2$
- Inelasticity (energy transfer in Lab):
 $\nu = (P \cdot q) / M_T$
- Bjorken variable:
 $0 < x = Q^2 / 2M_T \nu \leq 1$



- The differential cross section (unpolarized):

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{\alpha^2 E'}{Q^4 E} L_{\mu\nu} W^{\mu\nu}$$

lepton tensor (symmetric part):

$$L^{\mu\nu} = 2(k^\mu k'^\nu + k'^\mu k^\nu - k \cdot k' g^{\mu\nu})$$

hadronic tensor (symmetric part):

$$W^{\mu\nu} = W_1(x, Q^2) e^{\mu\nu} + [W_2(x, Q^2) / M_T^2] \tilde{P}^\mu \tilde{P}^\nu,$$

$$(e^{\mu\nu} = g^{\mu\nu} - q^\mu q^\nu / q^2, \quad \tilde{P}^\mu = P^\mu - (P \cdot q) q^\mu / q^2)$$

- Structure functions F1 and F2:

$$F_1(x, Q^2) = M_T W_1(x, Q^2), \quad F_2(x, Q^2) = (P \cdot q / M_T) W_2(x, Q^2)$$

- Bjorken limit:

$$F_{1,2}(x, Q^2) \xrightarrow{Q^2 \rightarrow \infty, \nu \rightarrow \infty, x: \text{fixed}} F_{1,2}(x) \quad \text{Bjorken scaling}$$



● What can we see in DIS ?



The approximate Q^2 -independence of the structure functions

→ the virtual photon sees point-like constituents in the target – **quarks**

→ using distributions of quarks and anti-quarks,

$$F_1(x) = \frac{1}{2} \sum_f e_f^2 [q_f(x) + \bar{q}_f(x)], F_2(x) = 2xF_1(x) \quad (\text{Callan-Gross relation})$$

The small **scaling violation** is calculated by pQCD.

DIS probes a current-current correlation in the target ground state.

In the Bjorken limit, the probed correlation is **light-like**:

$$y^\pm = (t \pm y_3) / \sqrt{2}, \quad y^- \rightarrow 0, \quad \vec{y}_\perp \rightarrow 0, \quad y^+ \approx \sqrt{2} / M_T x$$

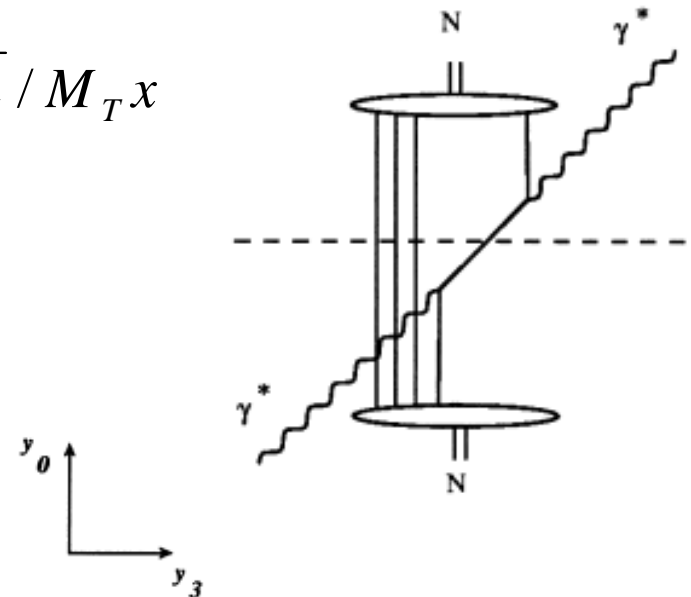
$$|t|, |y^3| \leq 0.2(\text{fm}) / x \approx \ell_c$$

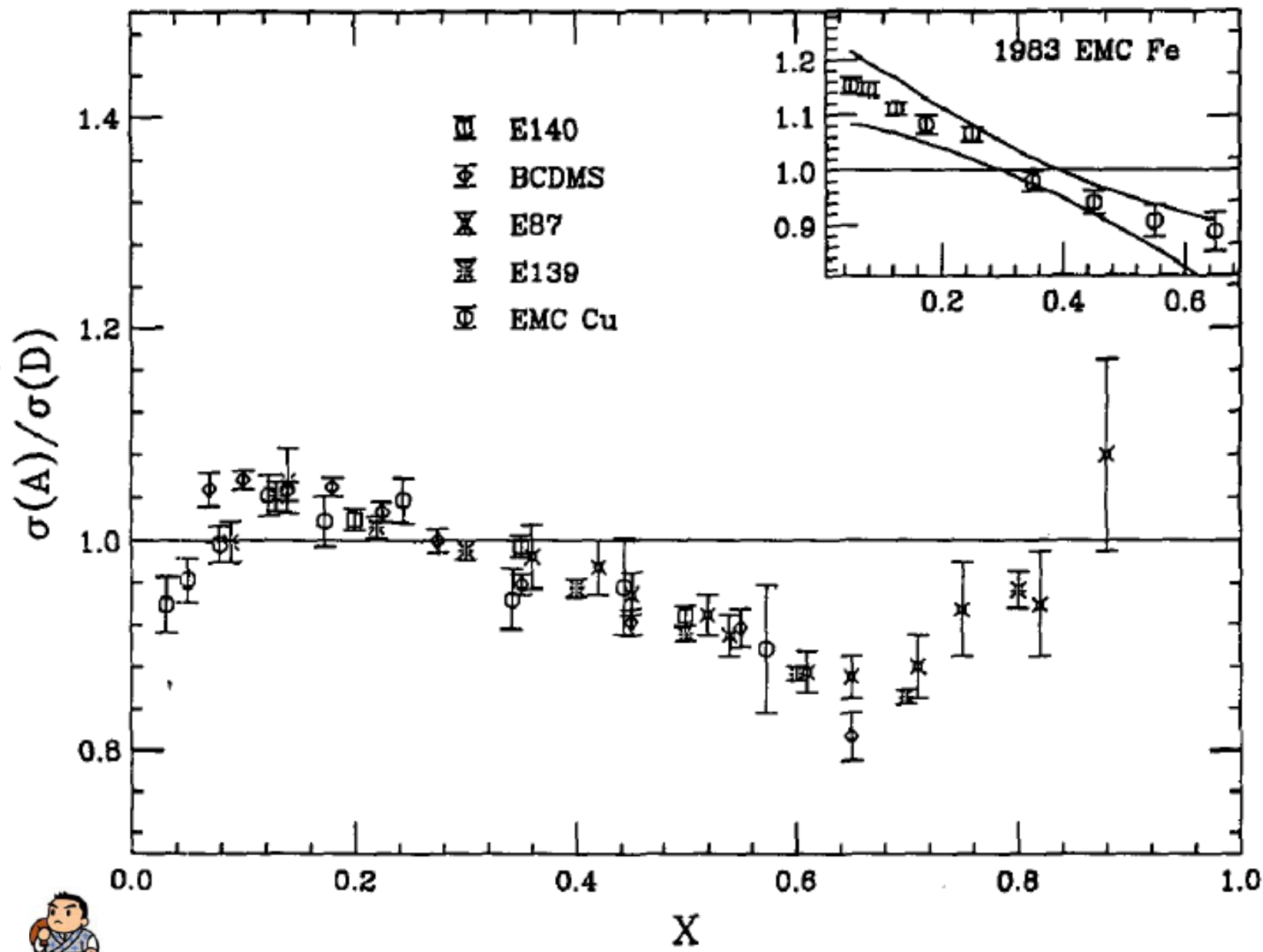
$$\sim 2.0(\text{fm}) \quad \text{for } x \sim 0.1$$

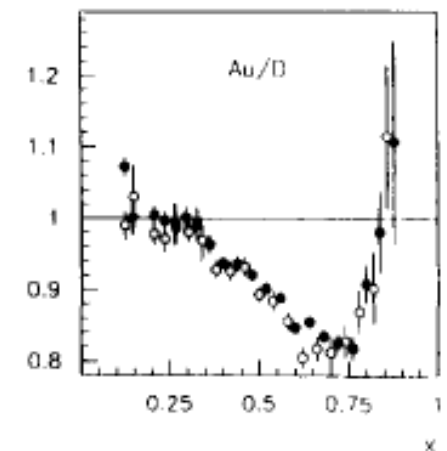
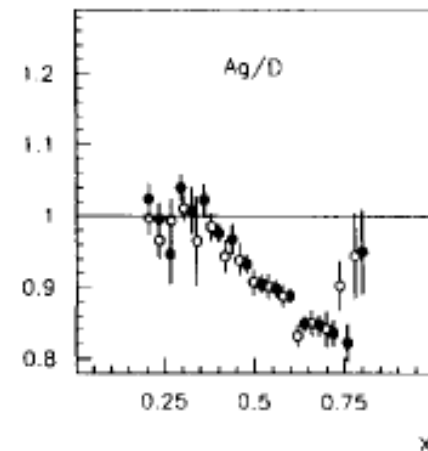
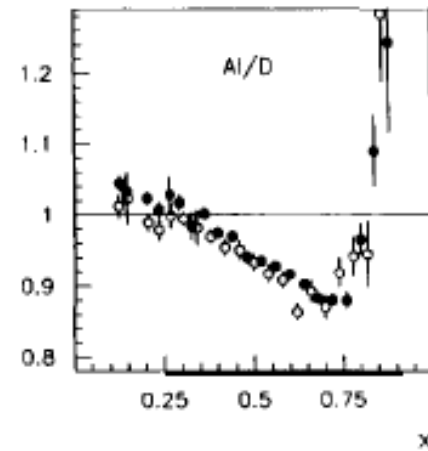
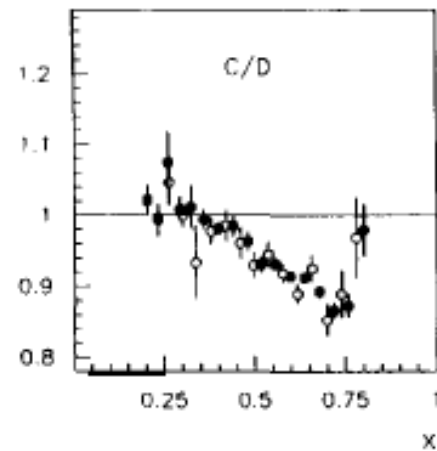
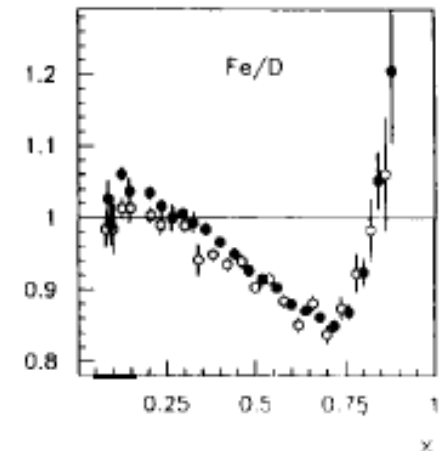
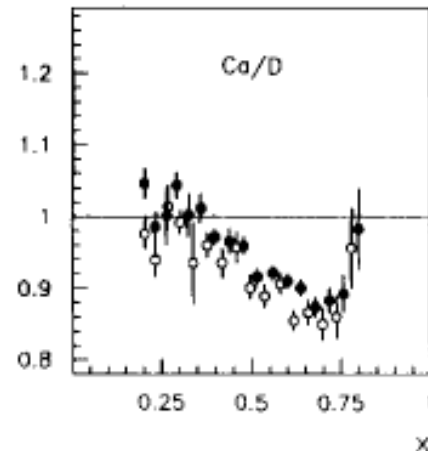
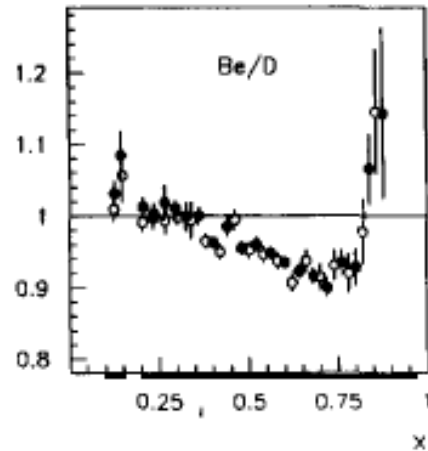
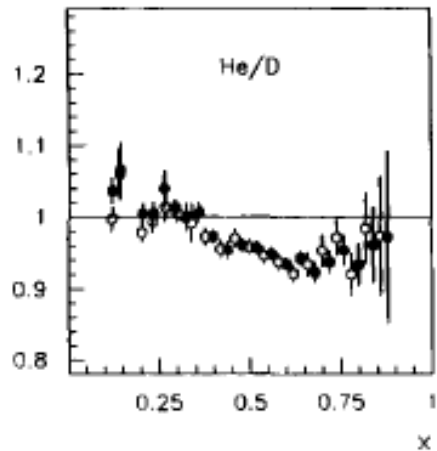
$$\sim 1.0(\text{fm}) \quad \text{for } x \sim 0.2$$

$$\sim 0.4(\text{fm}) \quad \text{for } x \sim 0.5$$

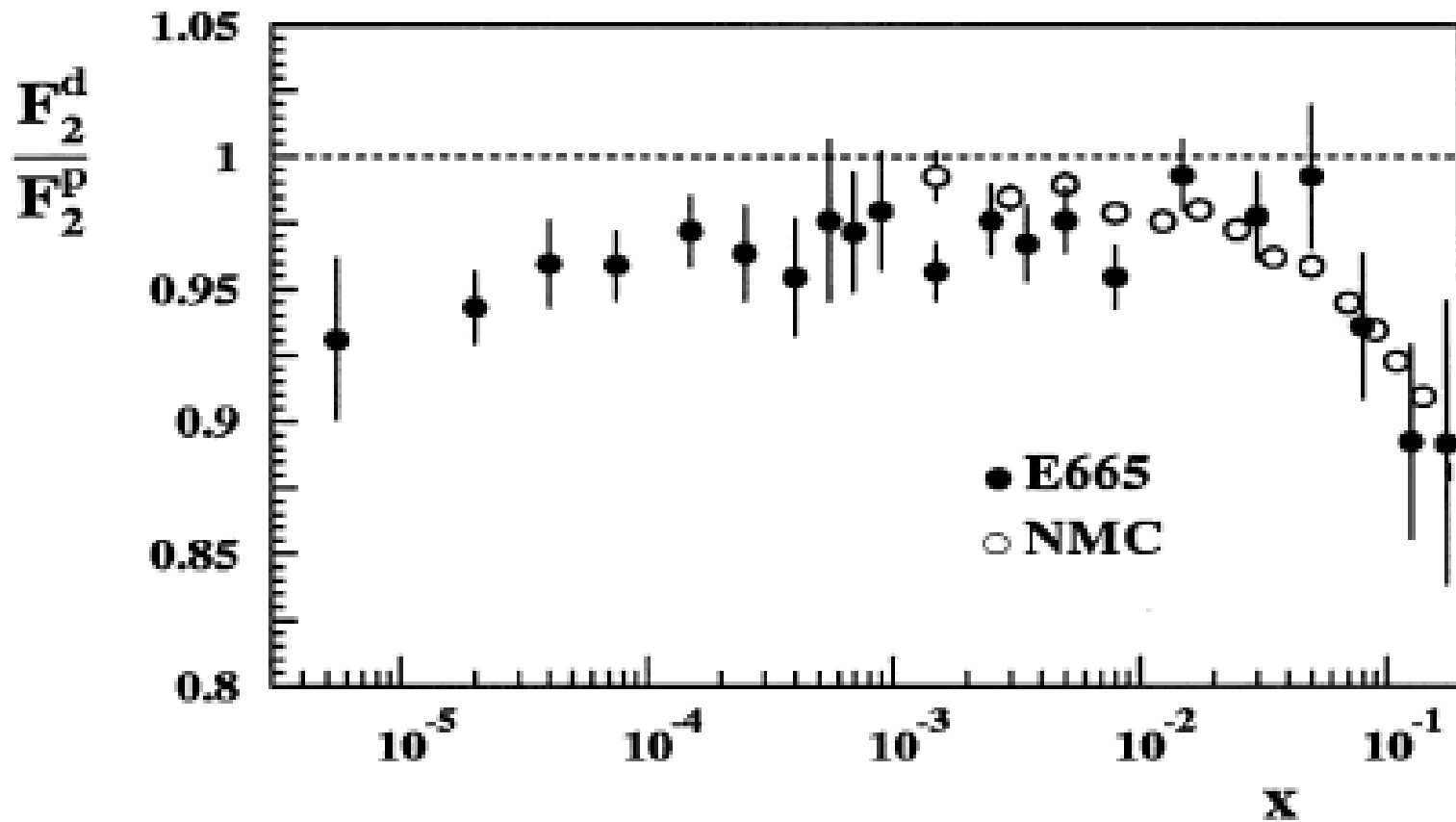
$$\sim 0.2(\text{fm}) \quad \text{for } x \sim 1.0$$







SLAC

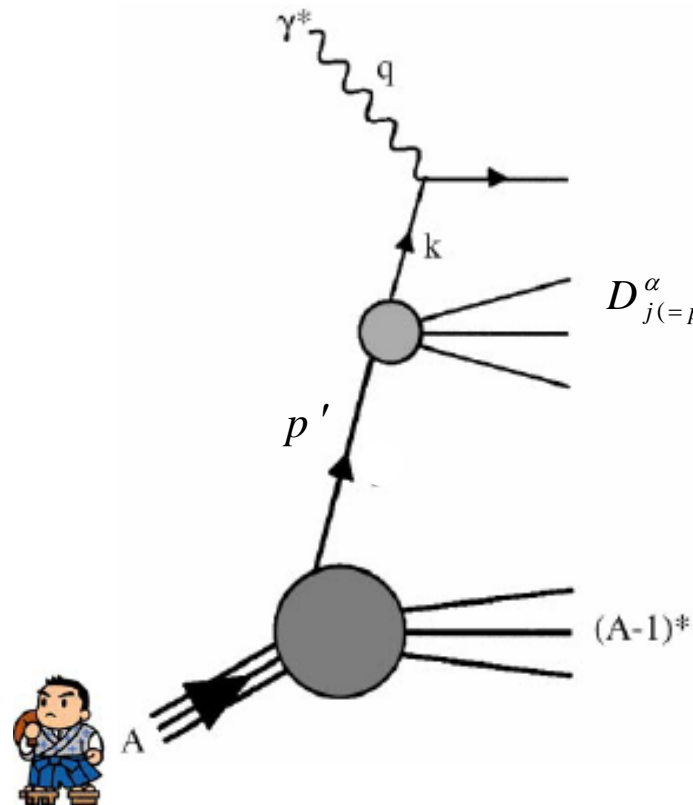


3. Theoretical approaches

- 3-1. Effect of the conventional nuclear physics — Binding and Fermi motion
- 3-2. Shadowing effect at small x
- 3-3. Anti-shadowing ?

3-1. Effect of the conventional nuclear physics — Binding and Fermi motion

How does the conventional nuclear physics affect $F_2(x)$?



The nucleon is scattered incoherently in case of

$$\ell_c \leq d \approx 2 \text{ fm} \rightarrow x \geq 0.1$$

The light-cone momentum distribution of N in A:

$$D_{j(=p,n)/A}^\alpha(y, p^2) = y \int \frac{d^4 p'}{(2\pi)^4} S_j^\alpha(p') \delta\left(y - \frac{p' \cdot q}{P_A \cdot q} \frac{M_A}{M}\right) \delta(p^2 - p'^2)$$

$$y \approx p'^+ / P_A^+$$

$$S^\alpha(p) = \langle (A-1)_\alpha, -\vec{p} | \hat{\psi}(0) | A \rangle$$

$$= 2\pi \delta(p_0 - M - \varepsilon_\alpha + T_R) |\psi_\alpha(\vec{p})|^2$$

Spectral function

Quasi-elastic reaction $A(e, e'p)A' \rightarrow \varepsilon_\alpha$

Koltun sum rule: $E/A = (T-e)/2$ (2body force only)

Convolution form:

$$f_{a/A}(x) = \sum_{j,\alpha} \int dy dz \delta(x - yz) \int dp^2 D_{j/A}^\alpha(y, p^2) f_{a/j}(z, p^2)$$

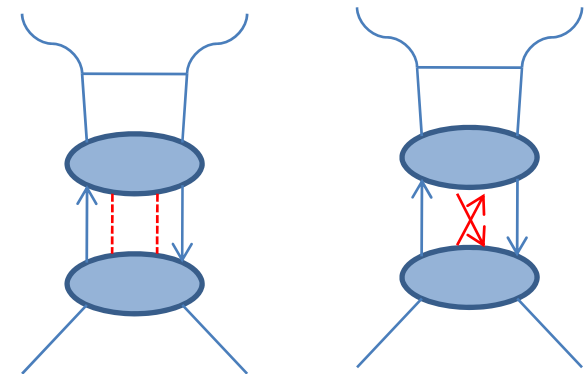
Assumptions in the convolution model:

- on-mass shell approximation $\rightarrow p^2 = M^2 \rightarrow$ if the binding is weak, OK?
- impulse approximation — final state interactions and interference terms are ignored

If OK, we get $F_2^A(x) = \sum_{j,\alpha} \int_x^A dy D_{j/A}^\alpha(y) F_2^j(x/y)$

Model-dependent calculations:

- ① Off-mass shell effect by Kulagin et al. ↓
- ② Final state interactions (q-ex.) by Hoodhoy et al. ↓
- ③ “Off-mass” shell (↓) + final state interaction (MFA) by Saito et al. ↑

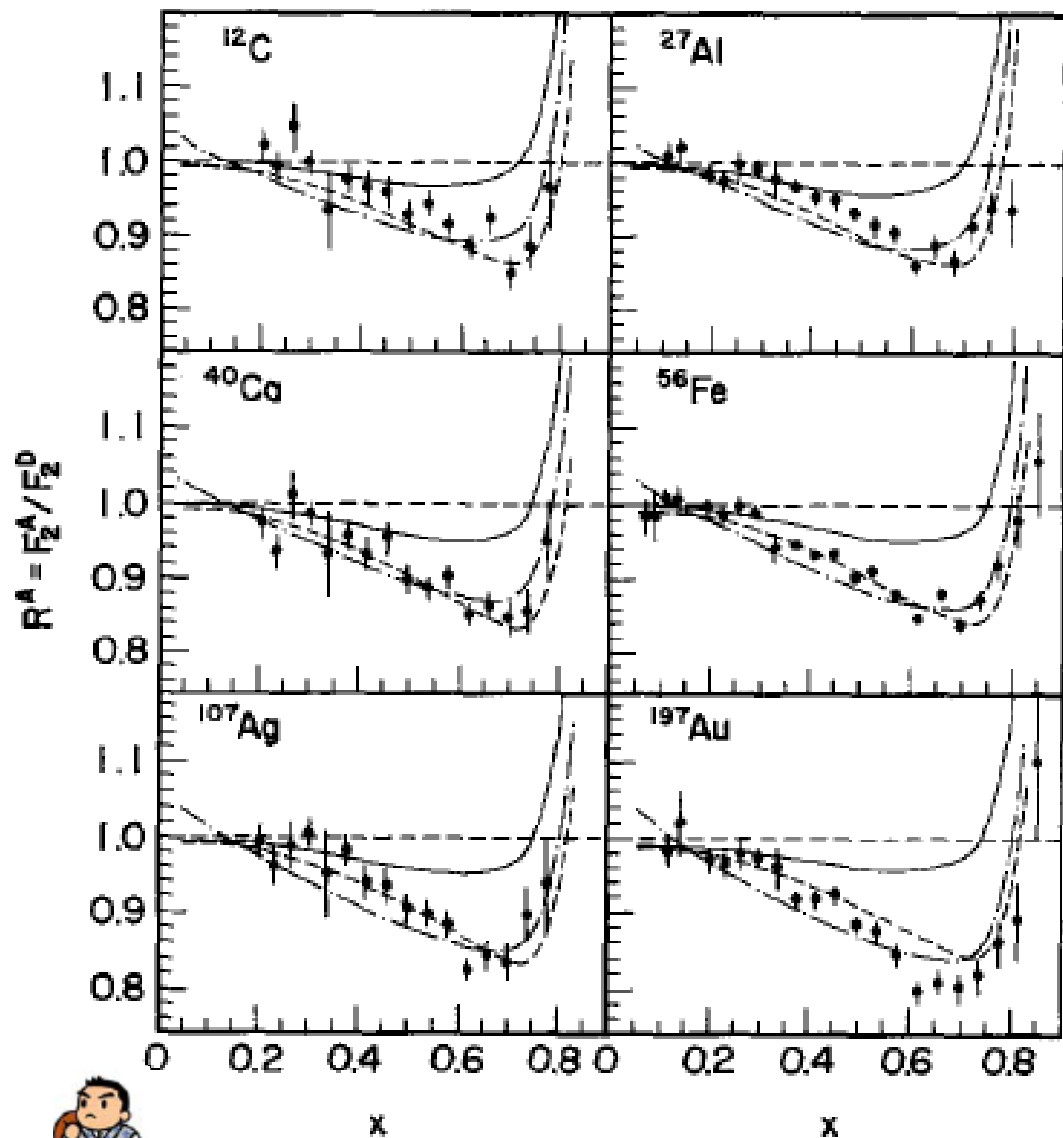


Ignored diagrams in the convolution

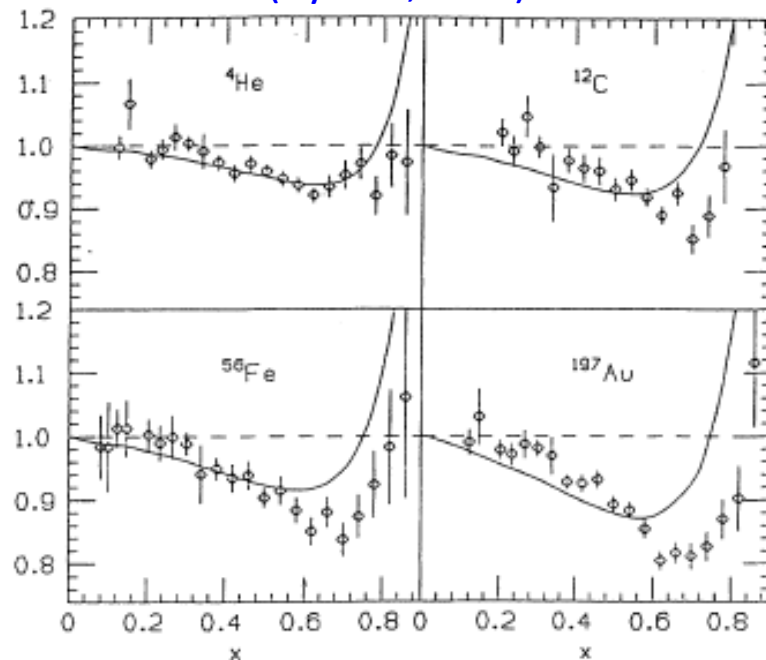
Note: Deuteron is also different from the average of proton and neutron — small EMC effect.



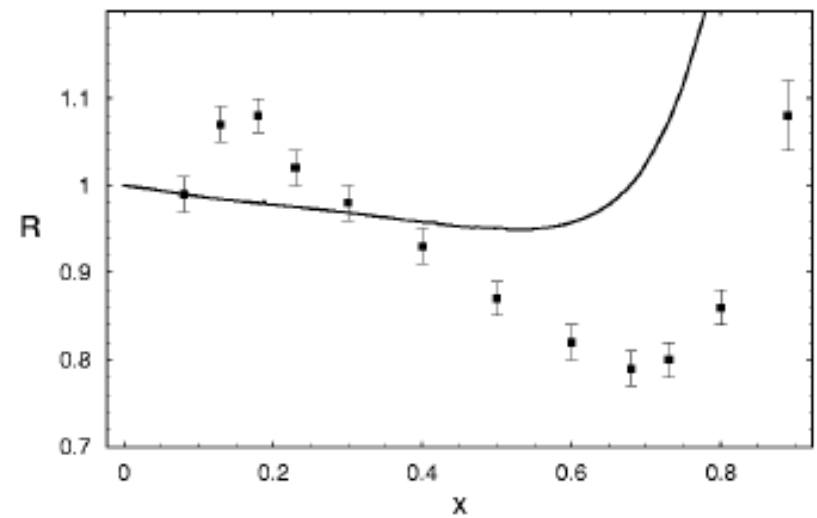
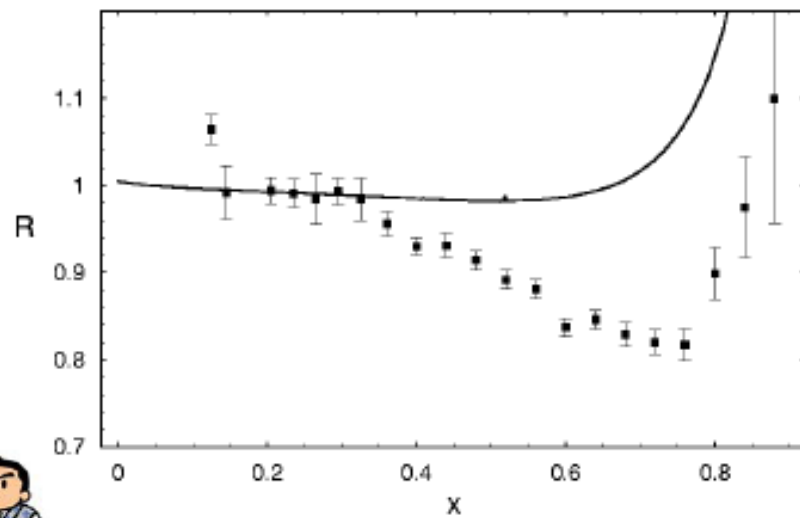
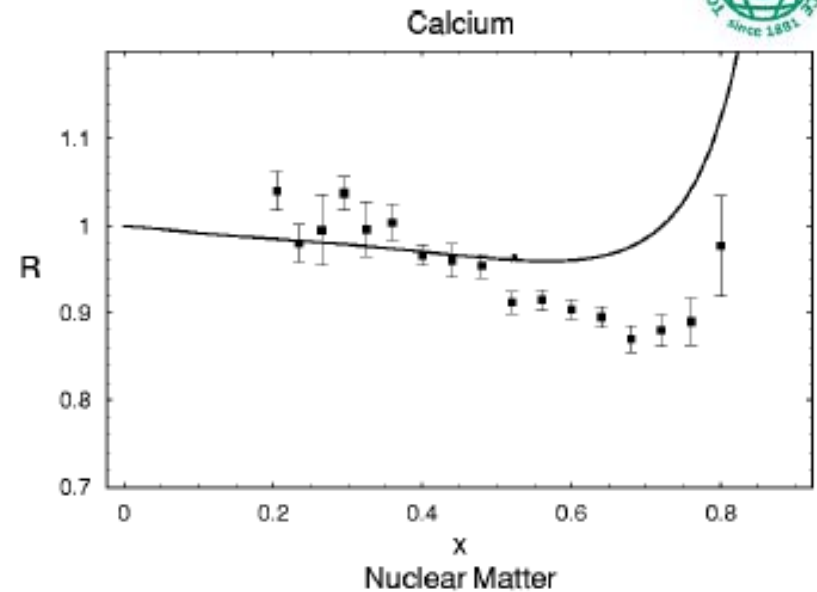
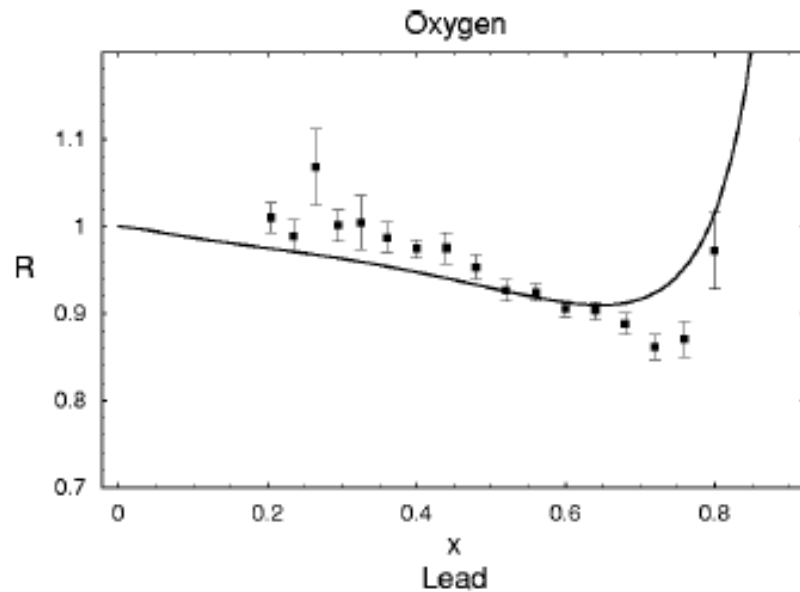
Nonrelativistic calculation (by Li, Liu, Brown)



(by Atti, Liuti)



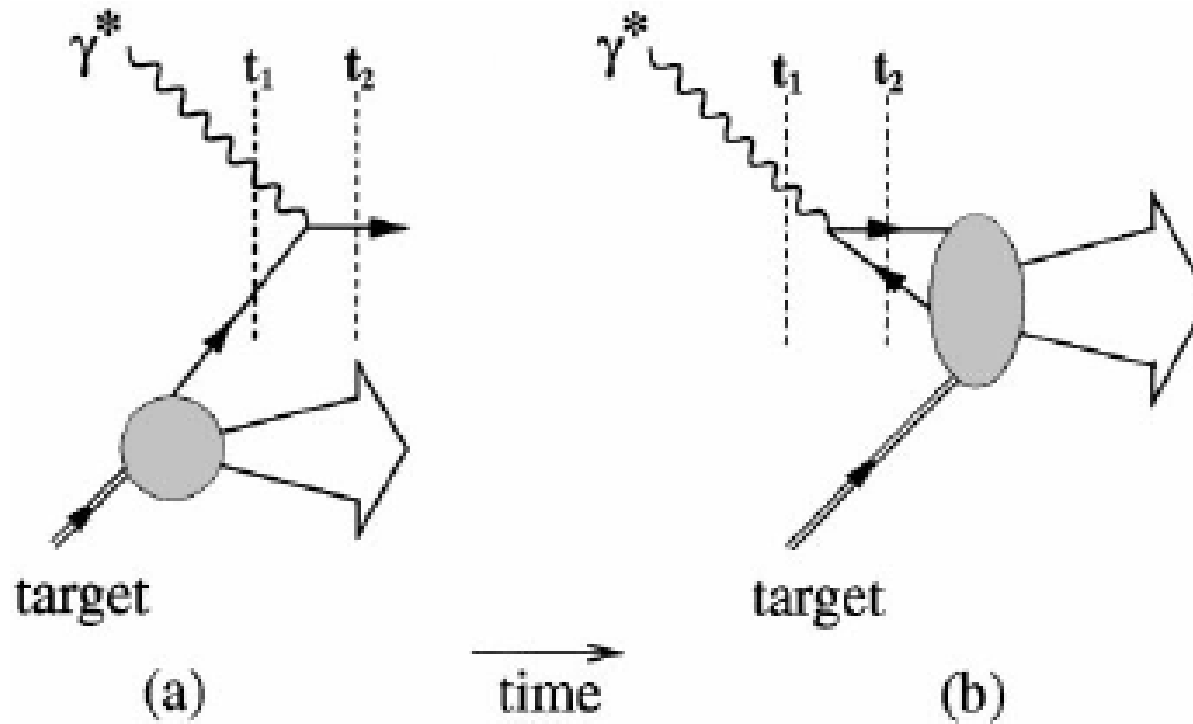
Relativistic calculation (by Smith, Miller)



3-2. Shadowing effect at small x

Shadowing region $\rightarrow \ell_c \geq d \approx 2 \text{ fm} \rightarrow x \leq 0.1$

DIS occurs coherently: $F_2^A(x) \approx \sigma_{\gamma^*A} < A \times \sigma_{\gamma^*N}$ ($\sigma_{\gamma^*A} \approx A^{0.8} \times \sigma_{\gamma^*N}$)



$$\left| A_a / A_b \right| \gg 1 \text{ for } x > 0.1$$

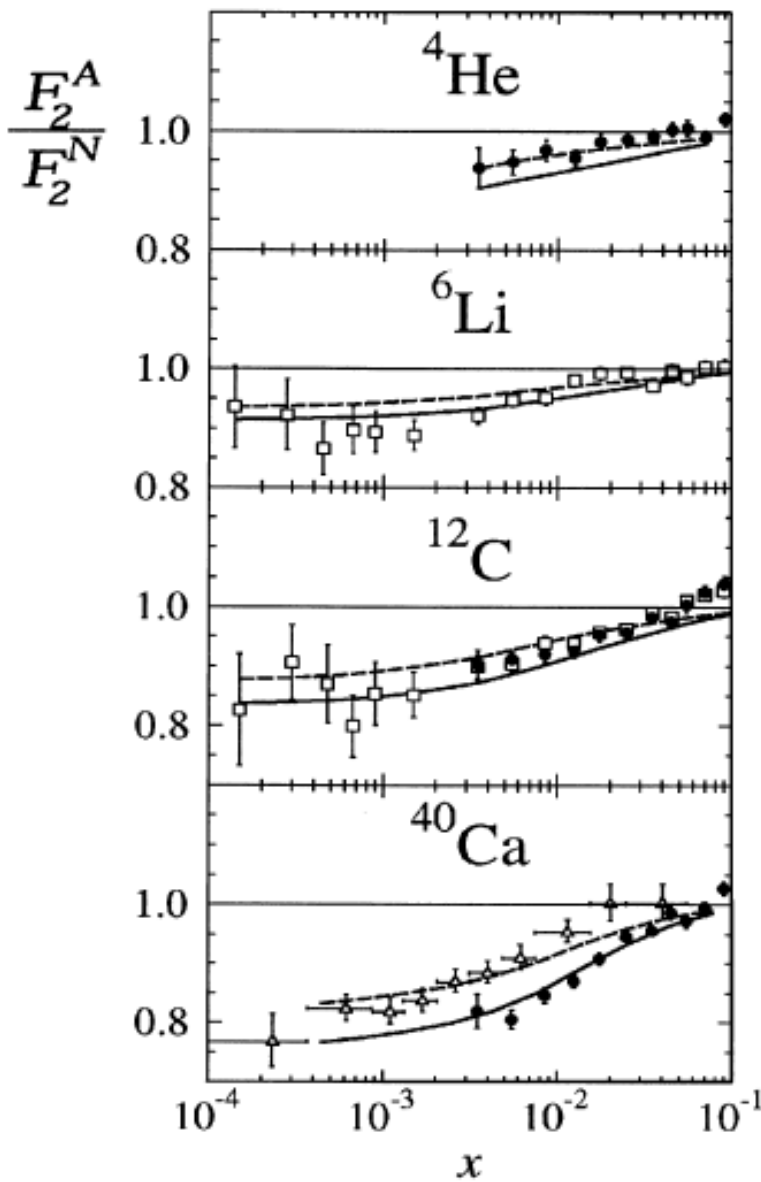
$$\ll 1 \text{ for } x < 0.1$$

for small x, the photon is supposed to be converted into vector mesons

VMD \rightarrow surface interaction $A^{2/3} \approx A^{0.8}$



Shadowing effect (by Piller et al.)



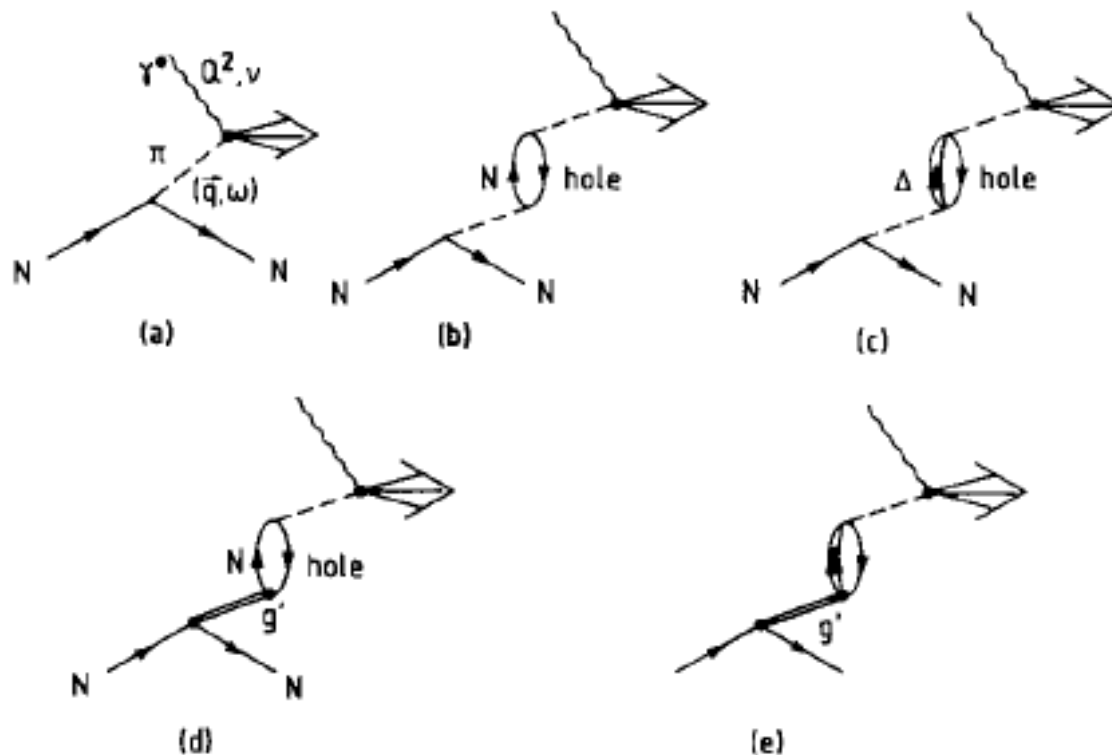
NMC+FNAL (ρ, ω, ϕ)



3-3. Anti-shadowing ?

Anti-shadowing region $\rightarrow 0.1 \leq x \leq 0.2$

An enhancement at small x region \rightarrow pion field enhancement ???

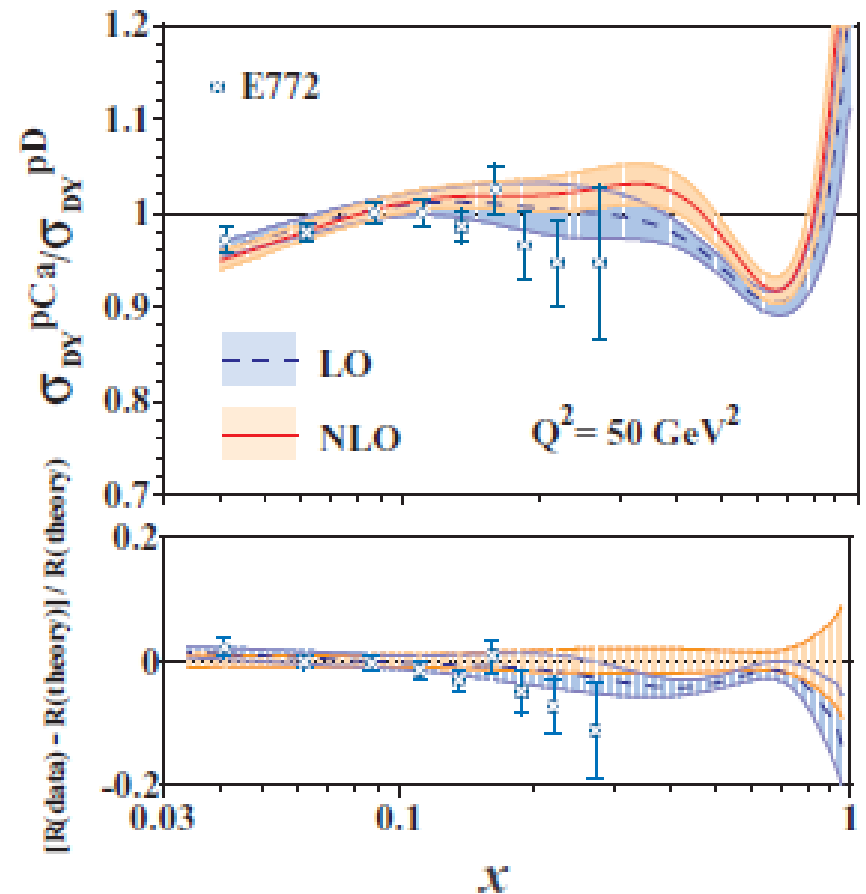
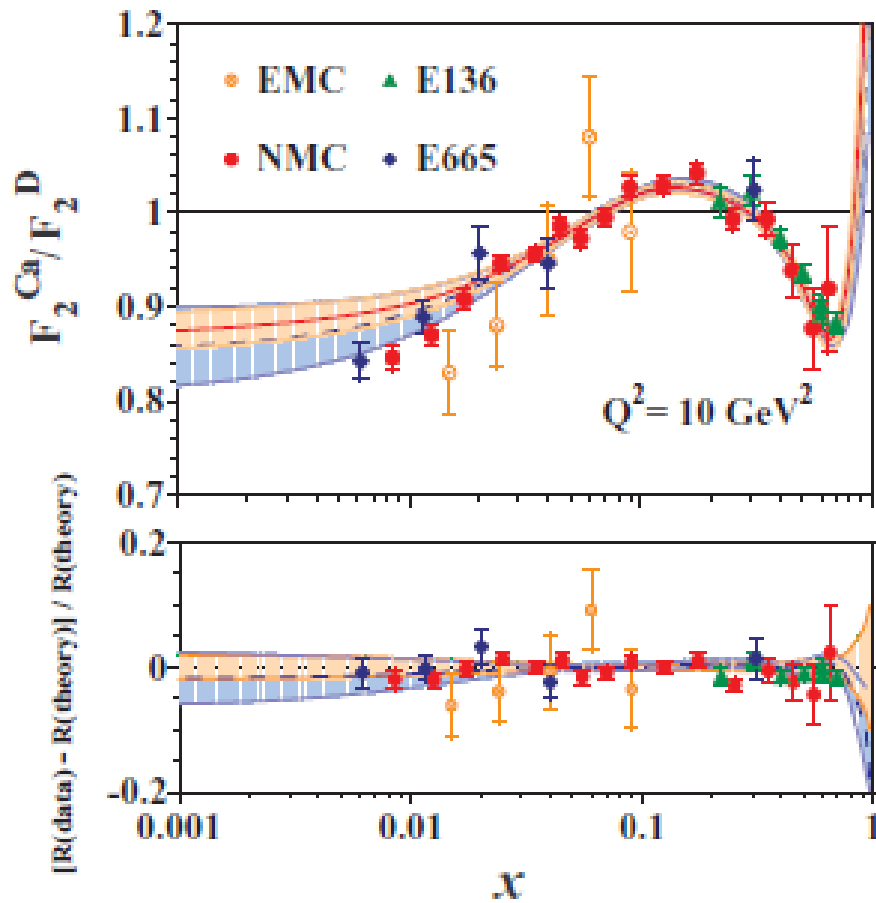


Recent data of the giant Gamow-Teller states \rightarrow the Landau-Migdal parameters

$$g'_{NN} \approx 0.59, g'_{N\Delta} \approx 0.18 + 0.05 g'_{\Delta\Delta}$$

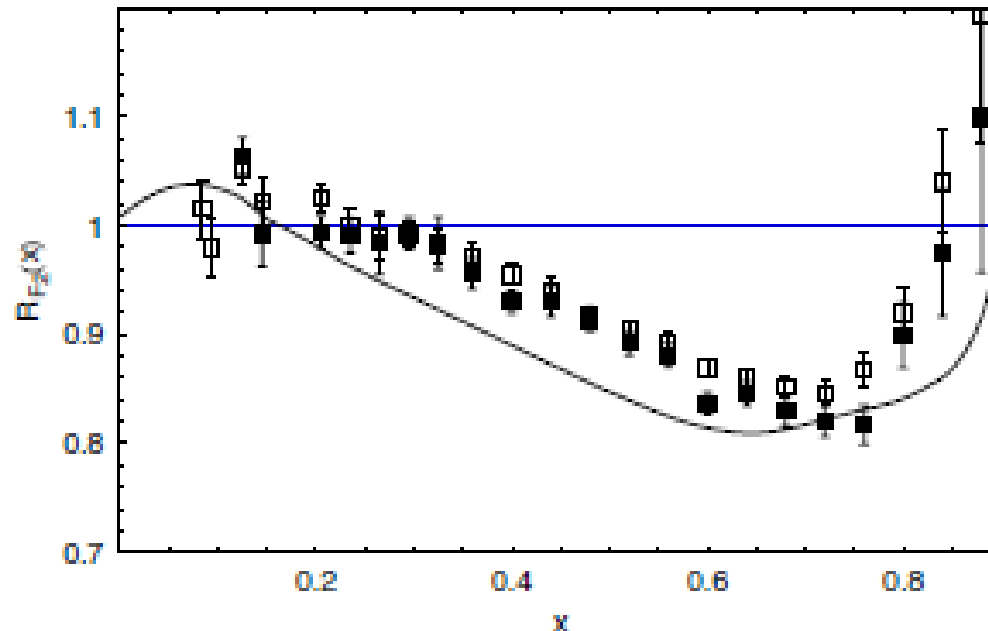


Parameterization of the EMC effect (by M. Hirai et al.)

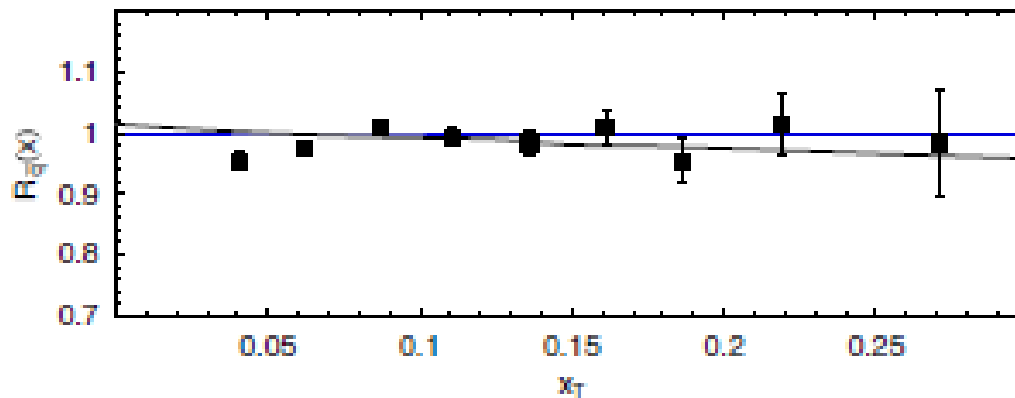


4. Possible explanations — what do we need ?

1. Chiral quark soliton model (by Smith and Miller)



SLAC-E139
Fe & Ag

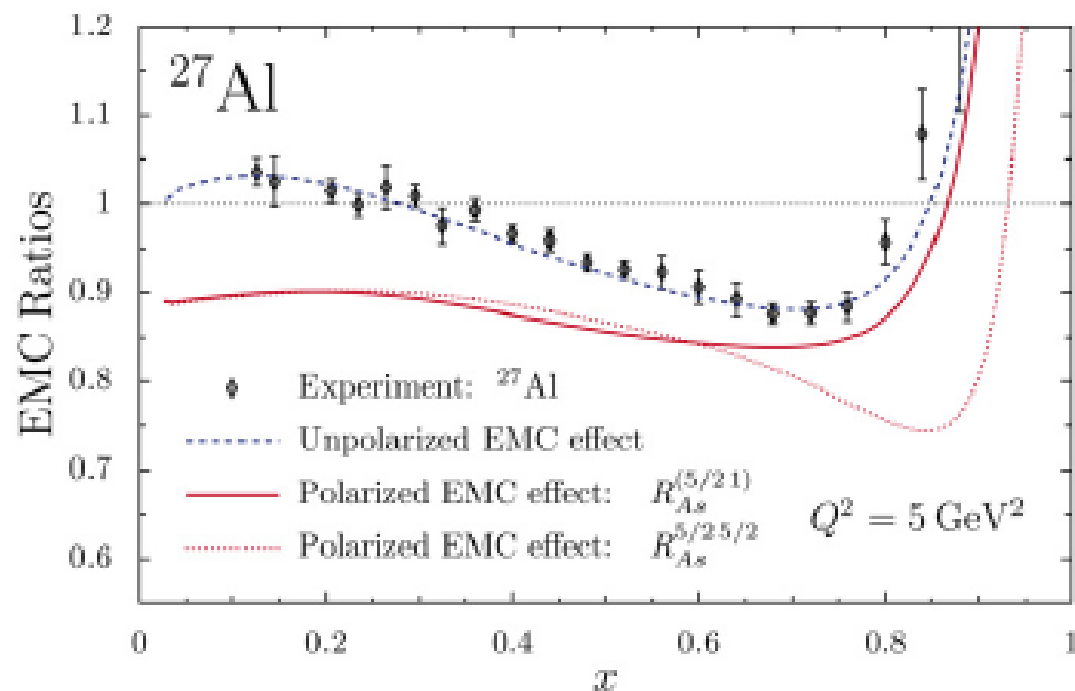
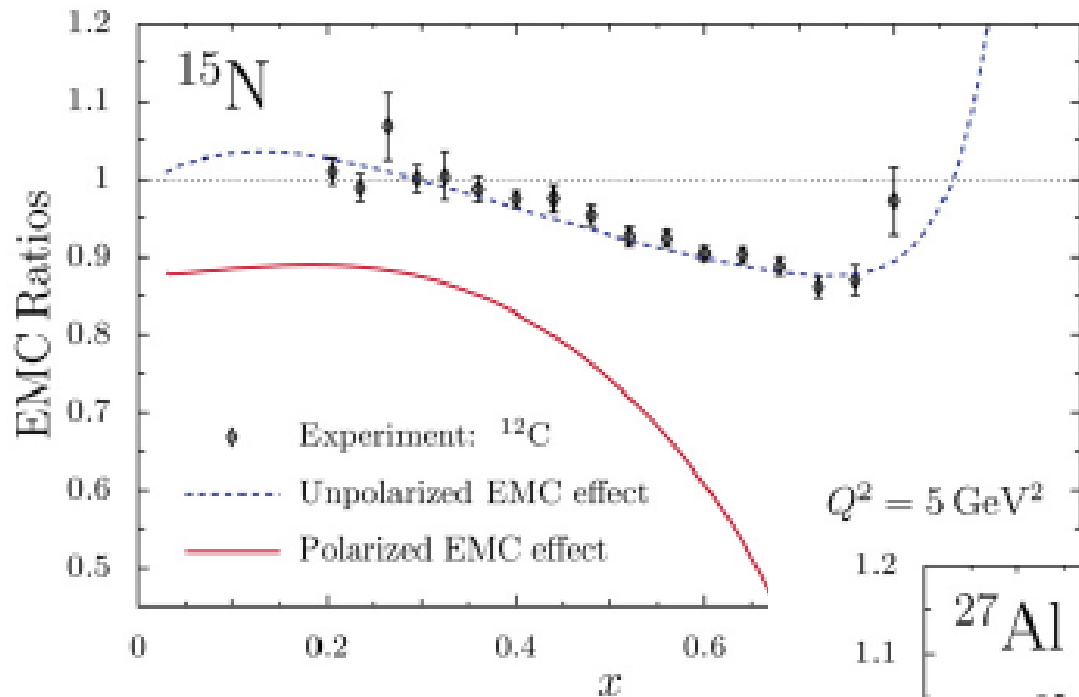


Drell-Yan exp.

FNAL-E772
W



2. NJL model (by Cloet et al.)



5. Summary

1. The quark distribution in a nucleus is different from that in the free nucleon:
 - about 20% reduction at $x \sim 0.7-0.8$
 - at small x , the structure function is reduced due to shadowing
 - for large x , the EMC ratio is very enhanced because of Fermi motion and short-range correlations
2. The energy-momentum distribution of a nucleon in a nucleus is vital to explain the EMC effect, but its effect is insufficient ?
 - the internal structure of a nucleon is modified in a nucleus ?
3. The sea quark is enhanced in a nucleus around $x \sim 0.15$?
 - cf. the Drell-Yan result
4. At large $x (>1)$, what happens ?

